

COMPARISON OF CONTACT STRESS OF A SPUR GEAR FOR DIFFERENT MATERIALS AND MODULES USING AGMA STANDARDS IN FEA

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Abstract

Gearing is one of the most critical components in mechanical power transmission systems. This paper explains about the comparison of the geometry of spur gears for different materials and modules by modeling and mathematical equations, load distribution at various positions of the contact line and the contact stress analysis of spur gears using three-dimensional finite element method. The contact stresses were examined using three-dimensional finite element model. These stresses of different modules for different materials obtained from the finite element analysis were compared with the theoretical values. Both results agree very well. This indicates that the finite element method model is accurate.

Key words: Gearing, transmission system, bending stresses, Root stresses, finite element method.

I. INTRODUCTION

Gearing is one of the most critical components in a mechanical power transmission system, and in most industrial rotating machinery. It is possible that gears will predominate as the most effective means of transmitting power in future machines due to their high degree of reliability and compactness [1]. In addition, the rapid shift in the industry from heavy industries such as shipbuilding to industries such as automobile manufacture and office automation tools will necessitate a refined application of gear technology [2].

A gearbox as usually used in the transmission system is also called a speed reducer, gear head, gear reducer etc., which consists of a set of gears, shafts and bearings that are factory mounted in an enclosed lubricated housing. Speed reducers are available in a broad range of sizes, capacities and speed ratios [3]. Their job is to convert the input provided by a prime mover (usually an electric motor) into an output with lower speed and correspondingly higher torque. The increasing demand for quiet power transmission in machines, vehicles, elevators and generators, has created a growing demand for a more precise analysis of the characteristics of gear systems. In the automobile industry, the largest manufacturer of gears, higher reliability and lighter weight gears are necessary as lighter automobiles continue to be in demand. Pitting is a surface fatigue failure resulting from repetitions of high contact stress [4]. The surface fatigue mechanism is not definitively understood. The contact-affected zone, in the absence of surface shearing tractions,

entertains compressive principal stresses. Rotary fatigue has its cracks grown at or near the surfaces in the presence of tensile stresses, which are associated with crack propagation, ends to catastrophic failure [5]. Fig. 1. shows the Nomenclature of gear

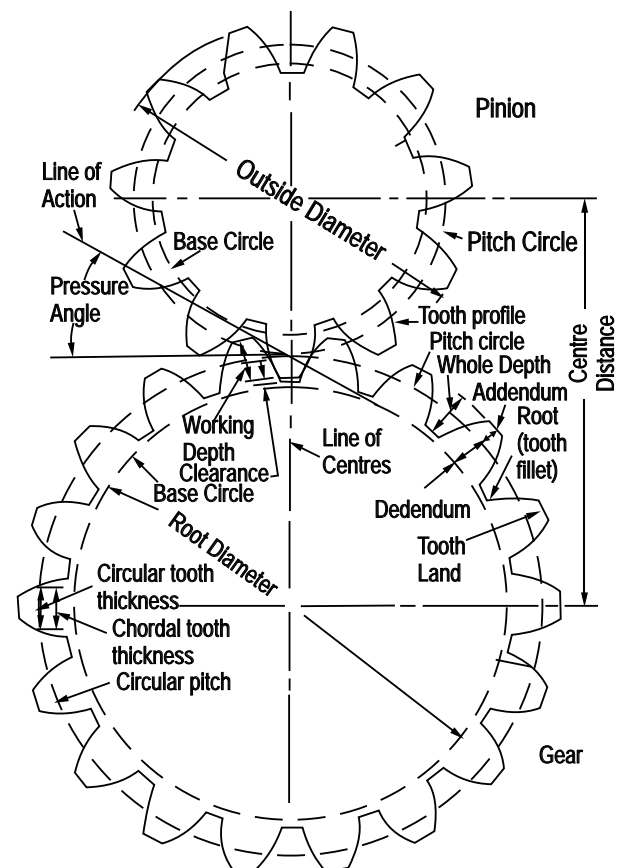


Fig. 1. Nomenclature of gear

The finite element method is proficient to supply this information but the time required to generate proper model is a large [6]. Therefore to reduce the modeling time a pre-processor method that builds up the geometry required for finite element analysis may be used, such as Pro/Engineer. Pro/Engineer can generate three dimensional models of gears. In Pro/Engineer the generated model geometry is opened in ANSYS for analysis [7]. The major cause of vibration and noise in a gear system is the transmission error between the meshing gears. By definition transmission error is the difference between the theoretical and the actual position between driving gear and the driven gear. It can be defined also as the amount by which the ratio at a given point in a revolution departs from the correct ratio.

II. SPUR GEAR DESIGN

The gear design problem are taken as, a pair of spur gears with pinion 17 teeth to transmit 25 kW at 1500 rpm. The gear has 44 teeth at 635 rpm and the material for gear pair is steel C45 as shown in Fig. 2. The pressure angle is 20° and module 6mm. The above problem the objective functions as follows:

Design Objectives. The design objectives considered in the gear design are, Minimization of the overall weight, Minimization of the centre distance, life expectancy. The objective functions are obtained in terms of design variables Normal module (m_n), material selection and Thickness of the gear (b) with the input parameters tabulated in Table 1.

Table 1 Required Input data for spur Gear design (Steel C45 material)

Description	Gear	Pinion
Material	Steel C45	Steel C45
Number of teeth(Z)	44	17
Young's Modulus(E)	2.10×10^5 N/mm ²	2.10×10^5 N/mm ²
Speed (N)	635rpm	1500rpm
Power (P)	25	25
Poisson Ratio	0.3	0.3
Normal Module (M)	6 mm	6 mm
Normal Pressure Angle	20°	20°

The gear design problem are taken as, a pair of spur gears with pinion 17 teeth to transmit 25 kW at 1500 rpm. The gear has 44 teeth at 635rpm and the material for gear pair is Steel 40Ni 2Cr1Mo28 as shown in Fig.3. The pressure angle is 20° and module 5mm. the input parameters tabulated in Table 2.

Table 2 Required Input data for spur Gear design (Steel 40Ni 2Cr1Mo28 material)

Description	Gear	Pinion
Material	Steel 40Ni 2Cr1Mo28	Steel 40Ni 2Cr1Mo28
Number of teeth(Z)	44	17
Young's Modulus(E)	2.15×10^5 N/mm ²	2.15×10^5 N/mm ²
Speed (N)	635rpm	1500rpm
Power (P)	25	25
Poisson Ratio	0.3	0.3
Normal Module (M)	5 mm	5 mm
Normal Pressure Angle	20°	20°

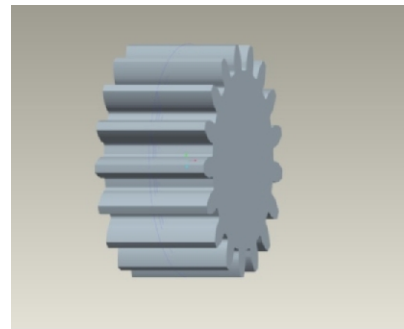


Fig. 2. Spur gear model for Steel C45

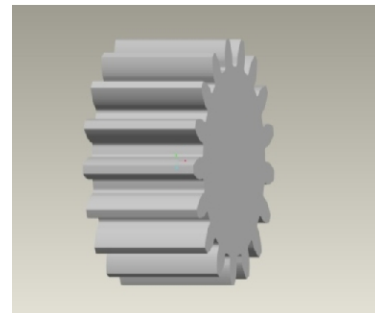


Fig. 3. Spur gear model for Steel 40Ni 2Cr1Mo28

Table 3 Results obtained as per AGMA Standard for spur Gear design

Description	Formula Used	Steel C45	Steel 40Ni 2Cr1Mo28
Pitch Diameter (D)	$m z_1$	102mm	85mm
Circular Pitch (Pc)	$\pi d_1/Z_1$	18.84mm	15.70mm
Diameter Pitch (Pd)	Z_1/d_1	0.16666	0.16666
Gear Ratio (i)	Z_2/Z_1	2.58	2.58
Centre Distance (a)	$\frac{m (Z_1 + Z_2)}{2}$	183mm	152.5mm
Pitch Line Velocity (v1)	$\frac{\pi d_1 N_1}{60}$	8.011m/sec	6.675m/sec
Force exerted (Ft)	$\frac{P}{v} k_o$	3120.67N	3745.31N
Transverse Force (Fr)	$F_t * \tan \phi$	1135.83N	1363.18N
Addendum	1m	6mm	5mm
Dedendum	1.25 m	7.5mm	6.25mm
Minimum total depth	2.25 m	13.5mm	11.25mm
Bottom Clearance	0.25 m	1.5mm	1.25mm
Fillet Radius at Root	0.4 m	2.4mm	2mm
Module (m)	$2C/(Z_1 + Z_2)$	6mm	5mm
Tip Diameter (da)	$(Z_1 - 2f_o) m$	114mm	95mm
Root Diameter (df)	$(Z_1 - 2f_o) m - 2c$	87mm	72mm
Initial Dynamic Load (Fd)	F_t / C_v	14023N	7917.54N
Velocity factor Cv	$6/(+ v)$	0.4058	0.473
Beam Strength (Fs)	$\pi * m * b * [\sigma_b] * y$	22.233*10 ³ N	31.510*10 ³ N
Accurate Dynamic Factor (Fd)	$F + \frac{21V(b * C + Ft)}{(21V + \sqrt{b * c + Ft})}$	21.863*10 ³ N	21.56*10 ³ N
Design Torque [Mt]	$M_t * K * K_d$	206.90N-m	213.10N-m
Contact Stress [σ_c]	$C_R * HRC * k_{cl}$	852.64N/mm ²	1142.5N/mm ²
Calculation of Centre Distance	$a \geq (1 + i)^2 \sqrt{\left(\frac{0.74}{\sigma_c}\right)} Z * \frac{E_{eq} [M_t]}{1\psi}$	155mm	141.08mm
Face Width b	ψa	58.56mm	44mm
Revision of design torque of gear [Mt]	$M_t * k * k_d$	297.05N-m	307.29N-m
Contact stress σ_c	$\sigma_c = 0.74(i + 1)/2 \sqrt{\left(\frac{1 + i}{ib}\right)} * E_{eq} [M_t]$	494N/mm ²	483N/mm ²

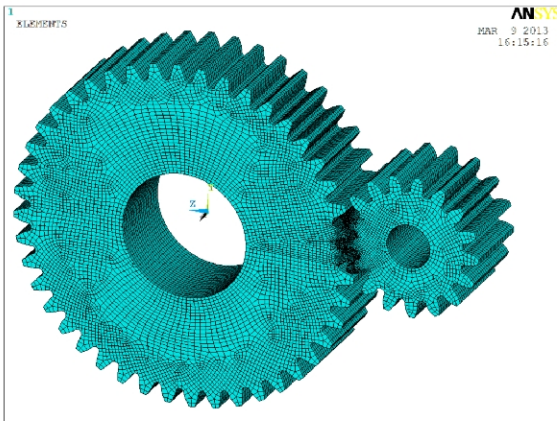


Fig. 4. Meshing of Spur gear for Steel C45

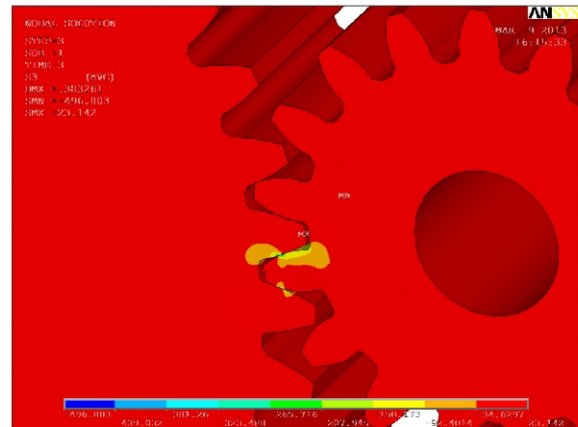


Fig. 7. Contact stress model of Spur gear for Steel C45

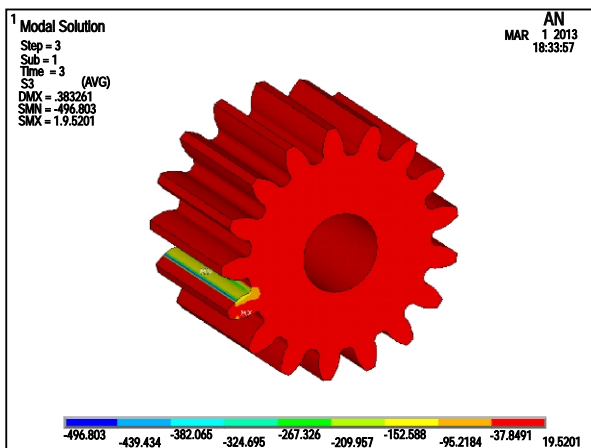


Fig. 5. Contact stress model of Spur gear for Steel C45

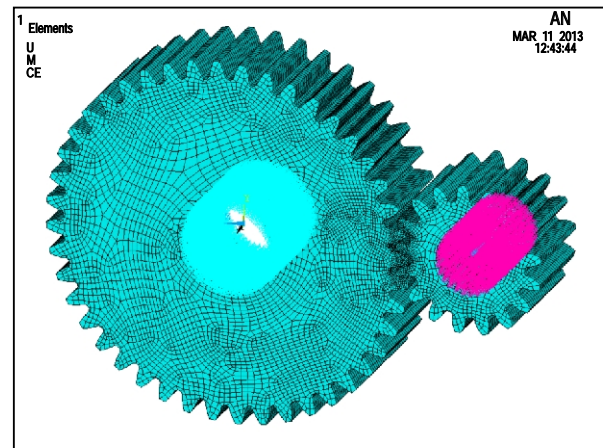


Fig. 8. Meshing of Spur gear for Steel 40Ni 2Cr1Mo28

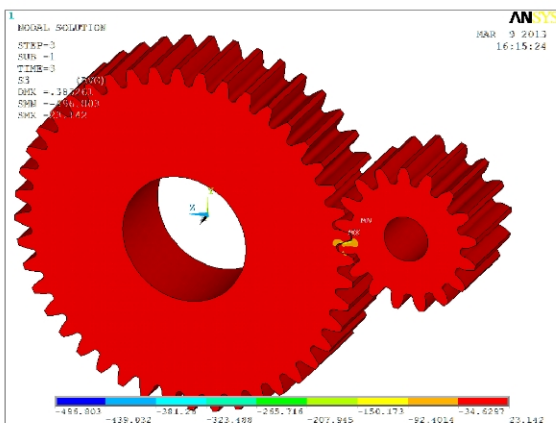


Fig. 6. Contact stress model of Spur gear for Steel C45

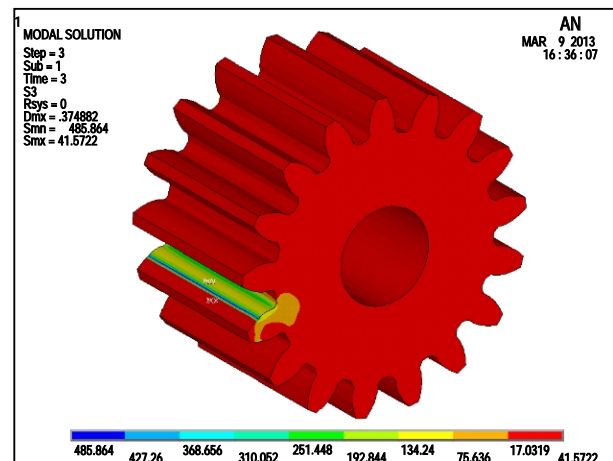


Fig. 9. Contact stress model of Spur gear for Steel 40Ni 2Cr1Mo28

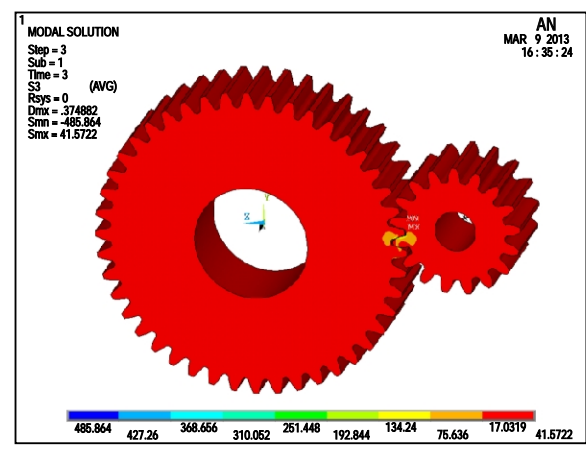


Fig. 10. Contact stress model of Spur gear for Steel 40Ni 2Cr1Mo28

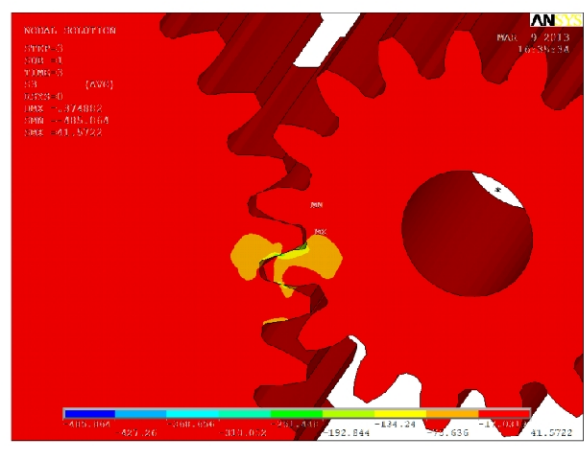


Fig. 11. Contact stress model of Spur gear for Steel 40Ni 2Cr1Mo28

Table 4. Comparison between Theoretical Value and FEA for spur Gear design

Description	Theoretical		FEA	
Material	Steel C45	Steel 40Ni 2Cr1Mo28	Steel C45	Steel 40Ni 2Cr1Mo28
Contact Stress	494 N/mm ²	483 N/mm ²	496.80 N/mm ²	485.86 N/mm ²

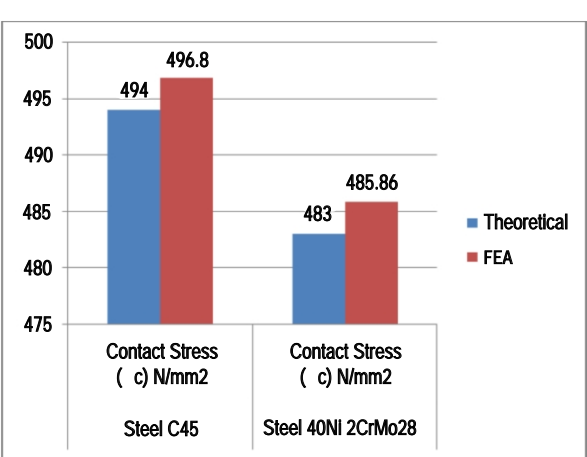


Fig. 12. Comparison between Theoretical value and FEA of spur gear for Steel C45 and Steel 40Ni 2Cr1Mo28

Table 3 shown the results obtained and they are explained through Fig. 4 to Fig. 11. Table 4. shows the comparison and it is explained in Fig. 12,

III. CONCLUSION

In the present study, effective methods to estimate the contact stress by the three-dimensional finite element method are proposed. To determine the accuracy of the present method for the contact stress three dimensional models were built in this paper. So those FEA models are good enough for stress analysis. The comparison results for the geometry of the spur gear of a two different module using three dimensional finite element analysis and theoretical calculation were obtained. The result reveals that the stress values computed theoretically and by finite element analysis were safe and within the allowable limit. The contact stress for steel C45 and Steel 40Ni 2Cr1Mo28 are within the allowable limit for both theoretical and finite element model methods. Both results agree very well. This indicates that the Finite element analysis model is accurate

NOTATIONS

- m_n : Normal Module in mm
- N_1, N_2 : Speed of Gear, Pinion in rpm
- P : Power transmitted in kW
- i : Gear (or) transmission ratio Gear in mm.
- b : Thickness of gear and pinion in mm

- a: Centre distance between shafts in mm
 z_1, z_2 : Number of teeth in pinion
 d_1, d_2 : Pitch circle diameter of pinion,
 α : Normal Pressure angle (helical gear)
 ρ : Density of the material in kg/mm^3
 E : Young's modulus in N/mm^2
 V_1 : Pitch Line Velocity
 $[M_t]$: Design twisting moment in N-mm
 y : Form factor
 f_o : Height factor
 k : Load concentration factor
 k_d : Dynamic load factor
 k_{bf} : Life factor for bending
 k_{σ} : Stress concentration factor for the fillet
 n : Factor of safety
 σ_c : Induced contact stress in N/mm^2
 $[\sigma_c]$: Allowable contact stress in N/mm^2

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